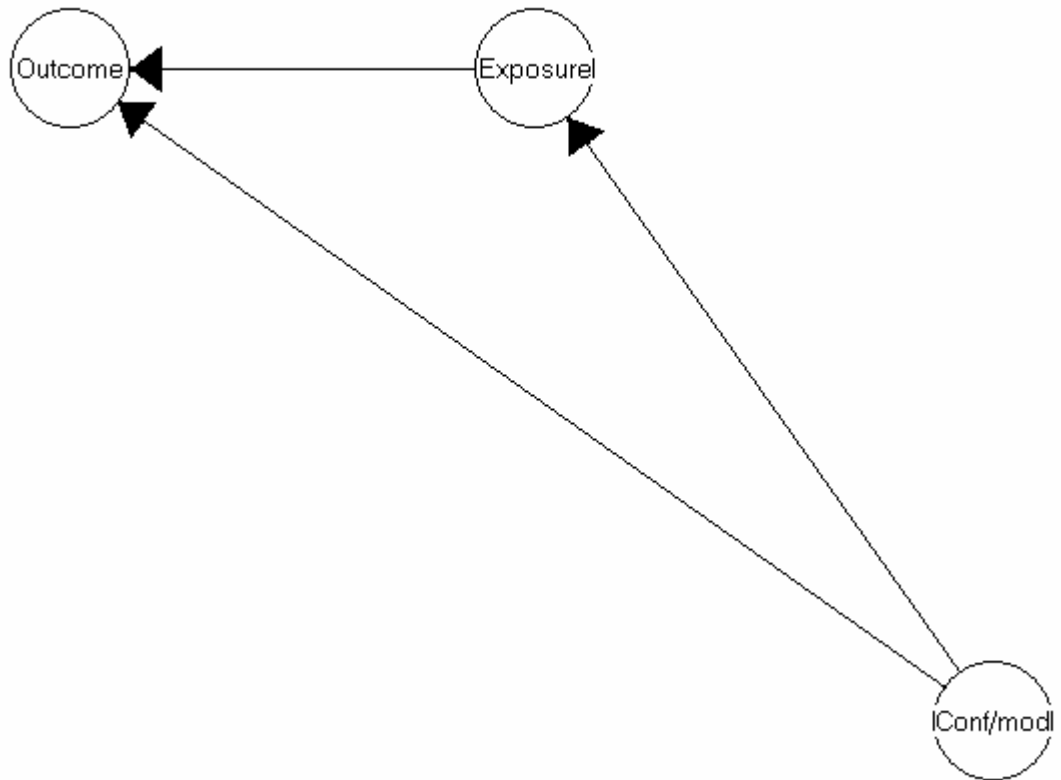


**Statistical models for causality  
in observational studies**

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## The typical epidemiological situation



Arrows indicate **causal** relationships

**The main problem: To estimate the causal effect of exposure on outcome taking confounding and effect modification into account.**

# Causality

**What do we mean when we say that there is a causal relationship between two variables?**

**What is the exact meaning of causal effect?**

**How do we avoid or adjust for the confounding effect of other variables?**

## Hill's causality criteria (Rothman & Greenland, 1998):

- Strength
- **Consistency** (repeated observations)
- Specificity
- **Temporality** (cause before effect)
- Biologic gradient
- **Plausibility** (subject matter arguments)
- **Coherence** (subject matter arguments)
- **Experimental experience**
- **Analogy** (subject matter arguments)

**Much epidemiological research is observational. Experimental evidence of causality therefore rarely exists.**

## **Philosophy of science (Suppes)**

**Discusses causality relative to events rather than statistical variables.**

**Causality may be deterministic or probabilistic?**

**(A probabilistic causal effect of A on B means that there is a deterministic effect of A on  $P(B)$ )**

**Prima facie probabilistic causes are**

**Spurious** if cause and effect are **conditionally independent** given events occurring before the cause

**Genuine** – if not spurious

## **What about statisticians?**

**Randomized experiments are required if we need evidence supporting a causal statement.**

**Current theory about causal models in statistics insists that:**

- 1) A causal model has to be a directed acyclic graph (DAG).**
- 2) Causal effects may be estimated from causal models of observational data.**

**Can causal order be determined by  
analysis of data?**

**Freedman's (1997) law of conservation of  
rabbits:**

**If you want to pull a rabbit out of the hat,  
you have to put a rabbit into the hat.**

**Remember,**

**Statisticians are making causal *models*,  
not causal theories.**

## **Davis' (1985) rules for causal modeling:**

**Rule 1a:** Run the arrow from X to Y if Y starts after X freezes.

**Rule 1b:** Run the arrow from X to Y if X is linked to an earlier step in a well-known sequence.

**Rule 1c:** Run the arrow from X to Y if X never changes and Y sometimes changes.

**Rule 1d:** Run the arrow from X to Y if X is relatively stable, hard to change, or fertile while Y is relatively volatile, easy to change, or has few consequences.



**Rule 2:** If there is a path starting from **X** and returning to it without retracing any steps, **X** and all the variables on the path form a loop. Variables in a loop have no order.

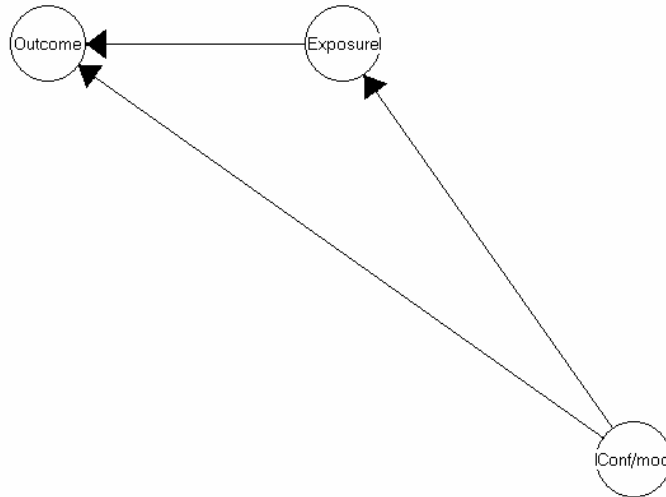
**Rule 3: Confounding.** If a prior variable has a causal path to the independent variable and a causal path to the dependent variable, it will contribute a statistical association between them that is causally spurious

**Rule 4:** Reversing poles for one variable reverses the signs of each of its relationships. Reversing polarities for both variables leaves the sign of their relationship unchanged.

**Rule 5:** The sign of a path is given by multiplying the sign of its arrows. A path of nonzero arrows will be positive unless it contains an odd number of negative arrows.

**Rule 6:** A System is inconsistent if at least one pair of variables has both positive and negative signs among its direct, indirect and spurious effects. Otherwise it is consistent.

# Causal effects



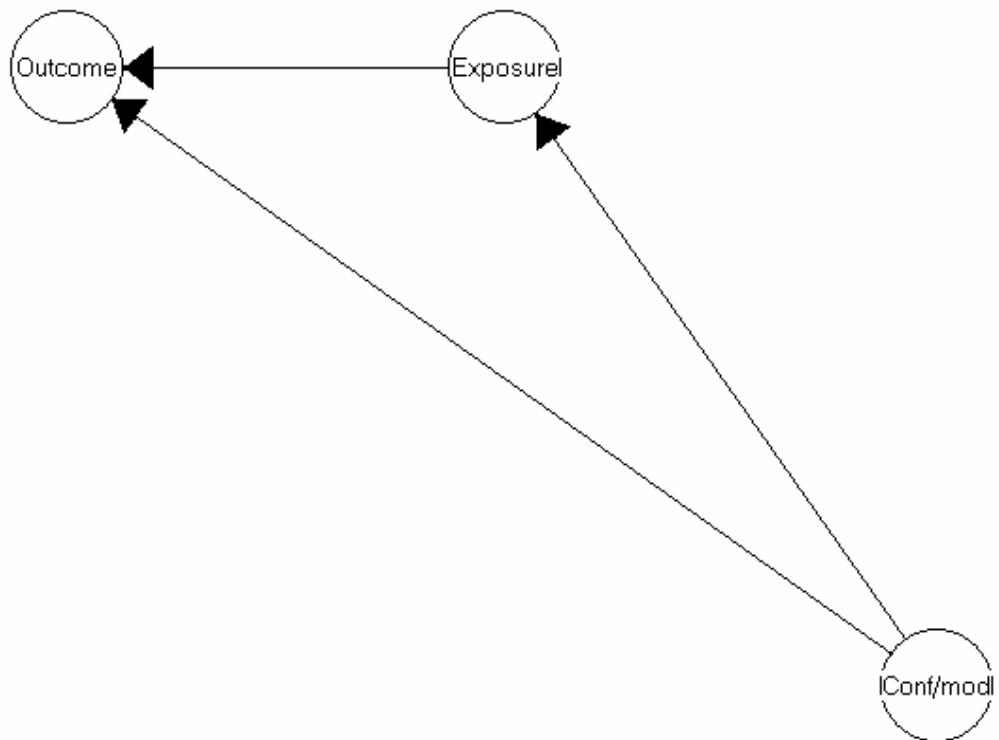
**How do we measure the causal effect of exposure on outcome?**

**Three types of causal effects**

**Total effects.**

**Direct effects**

**Indirect effects**



**The total effect of the confounder/mediator**

**=**

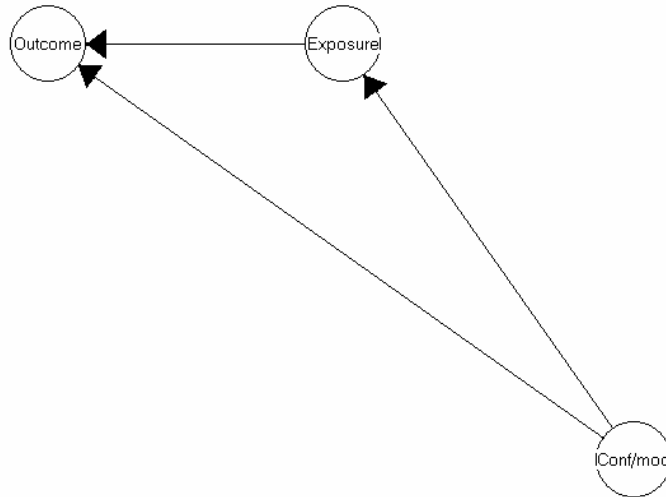
**Indirect effect mediated through Exposure**

**“+”**

**Direct effect**

**Common wisdom of epidemiologists tells us  
to disregard mediating variables**

# Causal effects



**How do we measure the causal effect of exposure on outcome?**

**Two types of causal effects**

**Individual local effects.**

**Average causal effects (ACE)**

## **Local (individual) effects**

**are defined by the conditional distribution of outcome (Y) given exposure (X) and **all** other risk factors:**

$$P(Y|X, Z_1, \dots, Z_k)$$

**The local effect of is a measure of the “distance” between two distributions**

$$\beta_{loc} = \text{dist}(P(Y|X=1, Z), P(Y|X=0, Z))$$

**The measure of effect may be confounded if the list of risk factors is incomplete, whether or not X is associated to the missing Zs**

**If the local effect differs across different values of Z then we say that Z modifies the causal effect.**

## **The average causal effect**

**If X is independent of all other risk factors then ACE is as a measure of the “distance” between the conditional distributions of Y given different values of X**

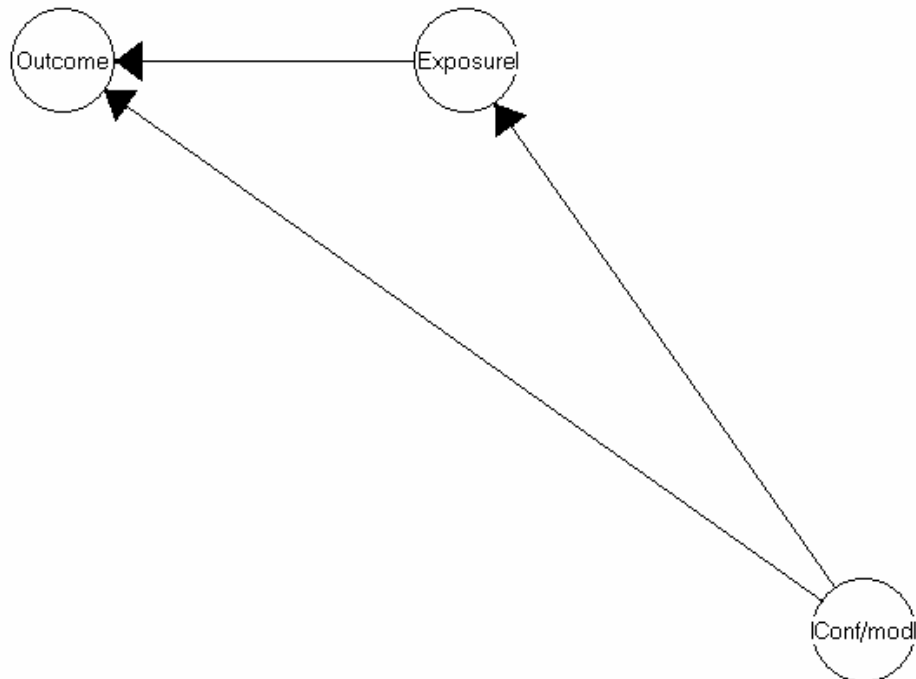
$$\beta_{ACE} = \text{dist}(P(Y|X=1), P(Y|X=0))$$

**ACE defined in this way is confounded if some risk factors are associated with X.**

**Calculation of ACE therefore in principle requires randomized experiments assuming that the local effects are the same**

**In practice, ACE may be estimated from observational studies if local effects are unconfounded.**

# Causal statistical models



**What kind of statistical model should we use to test and estimate the causal effect?**

**Local individual effects:**

**Dichotomous outcome: Logistic regression**

**Continuous outcome: Linear  
regression/ANOVA**

**There are, however, complications**



# Complications 1

## The nature of the outcome variable:

**Dichotomous**

**Frequent/infrequent events**

**Waiting times**

**Censored/not censored**

**Counts**

**Ordinal categorical variables**

**Summated scales**

**Quantitative measures**

## The model structure

**Multiple outcomes**

**Multiple exposures**

**Multiple confounders/modifacators**

**Intermediate variables**

# Complications 2

## Design problems

**Typical epidemiological studies are observational**

**Longitudinal studies are often not practical. Instead we use**

**Retrospective cross sectional surveys**

**Case control studies (consisting of retrospective surveys of Cases and controls)**

**Panel studies (repeated measurements)**

## Measurement problems

**Many risk factors are measured with errors**

# **Multivariate causal statistical models**

**Two options:**

**Structural equation models**

**Graphical models**